



# **Abstract Tree Regular Model Checking of Complex Dynamic Data Structures**

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November 6th, 2006

## Example program

```
// Doubly-Linked Lists
typedef struct {
    DLL *next, *prev;
} DLL;

DLL *DLL_reverse(DLL *x) {
    DLL *y,*z;
    z = NULL;
    y = x->next;
    while (y!=NULL) {
        x->next = z;
        x->prev = y;
        z = x; x = y;
        y = x->next
    }
    return x;
}
```

## Properties

- The usual properties of use of memory (absence of intrinsic errors)
- Shape invariants
  - Using **shape testers** like
 

```
x = aDLLHead;
while (x != NULL && random())
  x = x->next;
if (x != NULL && x->next->prev != x)
  error();
```
  - Using formulæ of a **logic** like

$$l \xrightarrow{next^*} [\exists x. p \xrightarrow{next} x \wedge x \neq \perp \wedge \neg(x \xrightarrow{prev} p)]$$

which can be translated into shape testers

## Verification approach

- Properties are translated to control line unreachability
- Verification using an automata-based framework
  - Encode memory configurations (shape graphs) as trees
  - Use finite-state tree automata to represent sets of configurations
  - Encode program statements as tree transducers (I/O automata)
  - Use Abstract Tree Regular Model Checking [BHRV '05]
    - \* Symbolic reachability analysis
    - \* Refinable abstractions on automata
- Implemented using Mona and applied to several case studies

# Overview

- Properties considered
- Automata based verification approach
  - Encoding of sets of memory configurations
  - Encoding of program statements as transducers
- Experiments

## Properties considered

- Basic consistency of pointer manipulations
  - absence of null and undefined pointer dereferences
  - no references to deleted nodes
- Shape invariance properties
  - like absence of sharing, acyclicity
  - if  $x \rightarrow \text{next} == y$  in a DLL then also  $y \rightarrow \text{prev} == x$
- Absence of garbage

## Specifying shape invariance properties

We describe negations of these properties

- Shape testers
- A logic of bad memory patterns
  - translated into shape testers

## Shape testers

- Instrumentation code written in **extended C**
  - following pointers backwards
  - non-deterministic branching
- Added to the program

Checking consistency of the next and previous pointers

```
x = aDLLHead;
while (x != NULL && random())
    x = x->next;
if (x != NULL && x->next->prev != x)
    error();
```

## A logic of bad memory patterns (LBMP)

- allows to describe bad shapes
- $\mathcal{V}$  finite set of program variables
- $\mathcal{S}$  finite set of selectors
- $\Phi ::= \exists w_1, \dots, w_n. \varphi$  with  $\mathcal{W} = \{w_1, \dots, w_n\}$  set of formulae variables
- $\varphi ::= \varphi \vee \psi \mid \psi, \psi ::= \psi \wedge \psi \mid x \varrho y \mid x \varrho$   
 $x, y \in \mathcal{V} \cup \mathcal{W}$  and  $\varrho$  is a reachability formula
- $\varrho ::= \xrightarrow{s} \mid \xleftarrow{s} \mid \varrho + \varrho \mid \varrho. \varrho \mid \varrho^* \mid [\sigma]$  where  $s \in \mathcal{S}$  and  $\sigma$  a local neighbourhood formula
- LNF:  $\exists u_1, \dots, u_m. BC(x \xrightarrow{s} y, x = y)$  with  $\mathcal{U} = \{u_1, \dots, u_m\}$  a set of local formula variables,  $s \in \mathcal{S}$ ,  $x \in \mathcal{V} \cup \mathcal{W} \cup \mathcal{U} \cup \{p\}$ ,  $y \in \mathcal{V} \cup \mathcal{W} \cup \mathcal{U} \cup \{p, \perp, \top\}$ ,  
 $p$  denotes the current position in the shape graph,  $\perp$  is NULL and  $\top$  undefined.

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- $\exists x. l \xrightarrow{next^*} [p = x] \xrightarrow{next} \xrightarrow{next^*} [p = x]$

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- $\exists x. l \xrightarrow{next^*} [p = x] \xrightarrow{next} \xrightarrow{next^*} [p = x]$

the list is cyclic

## Translation from LBMP to shape testers

- Suppose that all variables referred to in formula are reachable from  $\mathcal{V}$
- One starts by exploring the memory configurations starting from the variables
- go to special location if formula holds
- Disjunction : non-deterministic branching
- Conjunction : series of tests
- Reachability formulae  $\varrho ::= \xrightarrow{s} | \xleftarrow{s} | \varrho + \varrho | \varrho.\varrho | \varrho^* | [\sigma]$ 
  - $\xrightarrow{s} | \xleftarrow{s}$  : following the appropriate selectors (forward or backward)
  - $\varrho.\varrho$  : sequencing
  - $\varrho + \varrho$  and  $\varrho^*$  : non deterministic branching
- $[\sigma]$  can also be tested easily

## The verification problem

- If a basic consistency error is encountered, the program goes to some designated error location.
- Negations of shape invariance properties are expressed as formulæ of LBMP.
- They are translated into shape testers.
- If an error location is reached, the shape invariance property is broken.

Verification amounts to checking for control location unreachability

- Our approach: use abstract regular tree model-checking

## Regular Tree Model-Checking

[KMMPS '97, BT '02, AJMO '02, ALOR '05]

- Natural generalisation of Regular model-checking
- Configurations : trees (terms)
- Sets of configurations : finite tree automata (bottom-up)
- Operations: finite tree transducers (noted  $\tau$ )
- Basic verification problem : Computing the transitive closure of a finite tree transducer

## The verification problem

- Check:  $\tau^*(Init) \cap Bad = \emptyset$
- Compute  $\tau^*$  or
- For a given tree automaton  $A$ , compute  $\tau^*(A)$

## Abstract Regular (Tree) Model Checking

- Compute  $(\alpha \circ \tau)^*(Init)$  instead of  $\tau^*(Init)$

$$\tau^*(Init) \subseteq (\alpha \circ \tau)^*(Init)$$

- If  $(\alpha \circ \tau)^*(Init) \cap Bad = \emptyset$  then answer YES
- else if  $(\alpha \circ \tau)^*(Init) \cap Bad$  contains a **real** counterexample,  
then answer NO  
else refine the abstraction and start again

## Automata state collapsing as abstractions

- We define an equivalence relation  $\equiv$  on automata states
- We define an abstraction function  $\alpha(A) = A/\equiv$
- We propose several equivalence relations to define abstractions
  - States are equivalent if they accept the same trees up to some fixed height
  - States are equivalent if their languages have non-empty intersections with the same predicate tree automata.
  - States are equivalent if they are neighbours
- Refinement: choose finer equivalence relation

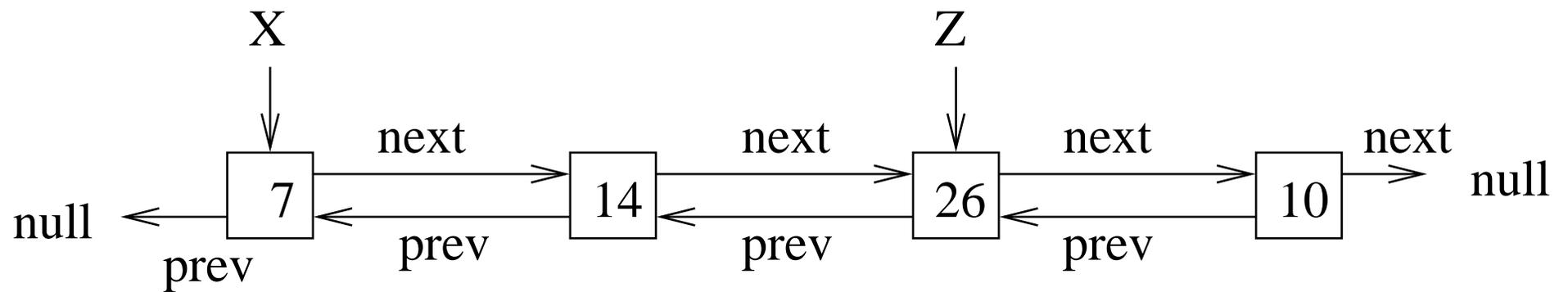
# Tree automata encoding of pointer manipulating programs

- Encoding of sets of memory configurations
- Encoding of program statements as transducers

## Encoding of shape graphs as trees

- $\mathcal{S} = \{1, \dots, k\}$  finite set of selectors,  $\mathcal{V}$  finite set of pointer variables
- A shape graph is a tuple  $SG = (N, S, V, D)$  where
  - $N$  is a finite set of memory nodes,
  - $N_{\perp, \top} = N \cup \{\perp, \top\}$
  - $S : N \times \mathcal{S} \rightarrow N_{\perp, \top}$  is a successor function
  - $V : \mathcal{V} \rightarrow N_{\perp, \top}$  is a mapping that defines where the pointer variables are currently pointing to, and
  - $D : N \rightarrow \mathcal{D}$  defines what (**finite**) data is stored in the particular memory nodes.

## Example of a shape graph



## Encoding of shape graphs as trees

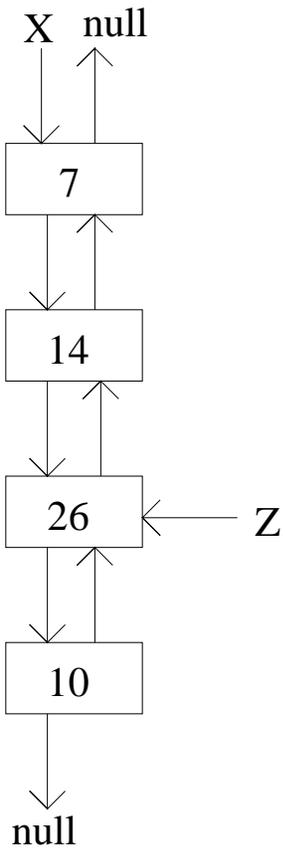
in the spirit of graph types [KS '93] and PALE [MS '02] but different

- Use trees as backbones
- describe links between nodes of the trees using pointer descriptors (with **routing expressions** expressing paths in the tree)

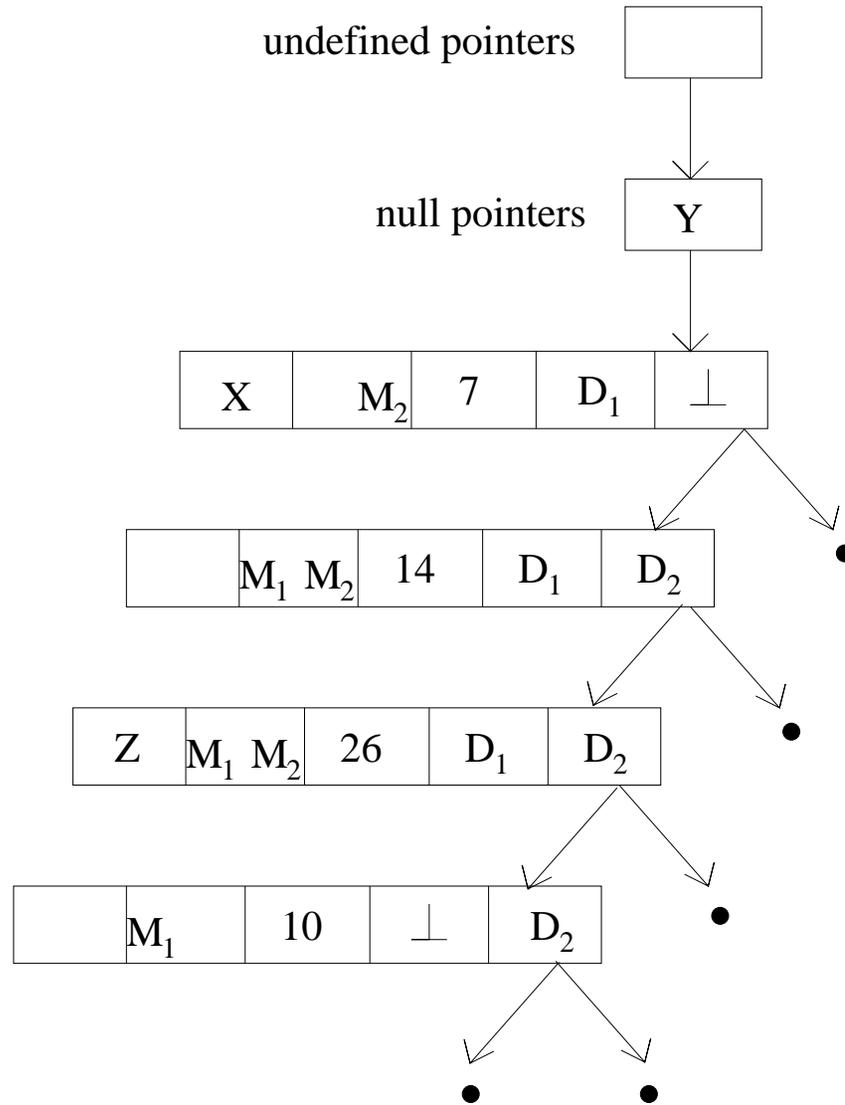
# Example

## The original DLL

Y → null



## A tree memory encoding of the DLL



## Descriptors

$$S = \{1, 2\} \quad S^{-1} = \{\bar{1}, \bar{2}\}$$

$$D_1 : 1.M_1$$

$$D_2 : \bar{1}.M_2$$

# Encoding

- Let  $\mathcal{S}^{-1}$  be the set of inverted selectors
- We fix a number of pointer descriptors
  - which have a unique marker (indicating where the pointer can point to)
  - with a routing expression describing paths in the tree backbone
- Each routing expression is a regular expression on the alphabet of pairs  $s.n \in (\mathcal{S} \cup \mathcal{S}^{-1}).\Sigma$  where  $\Sigma$  is the alphabet for nodes (data, markers, etc.)
- A tree memory encoding is a tuple  $(t, \mu)$  where  $t$  is a tree memory backbone and  $\mu$  a mapping from pointer descriptors to routing expressions.

## Encoding

- $\llbracket (t, \mu) \rrbracket$  is the **set** of shape graphs represented by  $t$ .
  - The nodes of the graph are internal nodes of the tree.
  - Links are obtained by following routing expressions
- A **tree automata memory encoding** is a tuple  $\llbracket (A, \mu) \rrbracket$  with a tree automaton  $A$
- A tree automata memory encoding represents the set of shape graphs  $\llbracket (A, \mu) \rrbracket = \bigcup_{t \in L(A)} \llbracket (t, \mu) \rrbracket$ .
- Remarks
  - The encoding is not canonical
  - $(A, \mu)$  and  $\llbracket (A, \mu) \rrbracket$  are two different notions
  - Given  $(A, \mu)$ ,  $\llbracket (A, \mu) \rrbracket$  can be empty although  $A$  is not empty.

## Encoding in Mona

- Use binary trees
- Routing expressions are “implemented” as tree transducers

## Encoding of program statements as transducers

- Each pointer manipulation statement is encoded as a tree transducer
- We add also the current program line (or error location) to the configuration
- Transducers are constructed such that they simulate the effect of program statements on the corresponding shape graphs

## Non-destructive updates and tests

- `x = null`
- `x = y`
- `if (x == null) then goto l1 else goto l2;`
- `x = y->s`
  - if `y->s` undef or null update `x` accordingly
  - else mark the `y` node with  $\blacklozenge$
  - apply corresponding routing expression transducer and move  $\blacklozenge$
  - remove `x` and put it into node marked by  $\blacklozenge$
  - can be non-deterministic if several targets are possible

## Destructive updates

$x \rightarrow s = y$

- To each statement like this a pointer descriptor is associated
- Add the particular pointer descriptor below  $x$
- Add the marker at  $y$
- Update the routing expression by adding the path from  $x$  to  $y$ 
  - take shortest path from  $x$  to  $y$
  - All possible paths will be added

## Dynamic allocation and reallocation

- `x = malloc()`
  - transform a leaf node
  - and add corresponding nodes for selectors
- `x.s = malloc()`
  - use the leaf node below `x`
  - and add simple routing expression
- `free(x)`

# Verification of programs with pointers using ARTMC

- Input structures

- start with a tree automata memory encoding (for example DLLs)
- start with empty shape graph and use a **constructor** written in C

```
aDLLHead = malloc();
aDLLHead->prev = null;
x = aDLLHead;
while (random()) {
    x->next = malloc();
    x->next->prev = x;
    x = x->next;
}
x->next = null;
```

- Applying ARTMC : Check for emptiness is not exact

## Experimental results

Example	Time	Abs. method	$ Q $	$N_{ref}$
SLL-creation + test	0.5s	predicates	22	0
SLL-reverse + test	6s	predicates	45	1
DLL-delete + test	8s	finite height	100	0
DLL-insert + test	11s	neighbour, predicates	94	0
DLL-reverse + test	13s	predicates	48	1
DLL-insertsort	3s	predicates	38	0
Inserting into trees + test	12s	predicates	91	0
Linking leaves in trees + test	11m15s	predicates	217	10
Inserting into list of lists + test	27s	predicates	125	1
Deutsch-Schorr-W. tree traversal	3m14s	predicates	168	0

SLL: Singly-linked list, DLL: Doubly-linked list

## Conclusion and further work

- new, automatic method for verification of programs with complex dynamic data structures
- Optimising the prototype implementation
- Checking absence of garbage
- Show termination