

Diffie Helman

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Summary: The Diffie Helman key exchange algorithm.

Protocol specification (in common syntax)

```
A, B :          principal
P, G, Xa, Xb :  number
one :           -> number
kap :           number, number, number -> number

1.  A -> B :     P, G
2.  A -> B :     kap(P, G, Xa)
3.  B -> A :     kap(P, G, Xb)
4.  A -> B :     {one()}kap(P, kap(P, G, Xb), Xa)
```

Description of the protocol rules

The function `kap` must satisfy:

$$\text{kap}(P, \text{kap}(P, G, Y), X) = \text{kap}(P, \text{kap}(P, G, X), Y)$$

It is implemented by: $\text{kap}(P, X, Y) = \exp(X, Y) \bmod P$.

It the protocol, `P` is choosen to be a prime number `P` and `G < P`.

The fresh symmetric key exchanged is $\text{kap}(P, \text{kap}(P, G, Xb), Xa) = \text{kap}(P, \text{kap}(P, G, Xa), Xb)$.

Requirements

The protocol must guaranty the secrecy of the fresh key.

The protocol must guaranty the authenticity of the participants.

References

[DH76]

Claimed proofs

[Bla01]

Claimed attacks

The authenticity is not guaranteed by the protocol.

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|----|------|----|------|---|-------------------------------------------------------------|----|
| 1. | I(A) | -> | B | : | P, G | |
| 2. | I(A) | -> | B | : | $\text{kap}(P, G, X_i)$ | |
| 3. | B | -> | I(A) | : | $\text{kap}(P, G, X_b)$ | or |
| 4. | I(A) | -> | B | : | $\{\text{one}()\}\text{kap}(P, \text{kap}(P, G, X_b), X_i)$ | |
| | | | | | | |
| 1. | A | -> | I(B) | : | P, G | |
| 2. | A | -> | I(B) | : | $\text{kap}(P, G, X_a)$ | |
| 3. | I(B) | -> | A | : | $\text{kap}(P, G, X_i)$ | |
| 4. | A | -> | I(B) | : | $\{\text{one}()\}\text{kap}(P, \text{kap}(P, G, X_i), X_a)$ | |

Citations

- [Bla01] Bruno Blanchet. An efficient cryptographic protocol verifier based on prolog rules. In IEEE, editor, *14th IEEE Computer Security Foundations Workshop (CSFW-14)*, june 2001.
- [DH76] W. Diffie and M. Helman. New directions in cryptography. *IEEE Transactions on Information Society*, 22(6):644–654, november 1976.